



CHAPTER 4

SAVING AND INVESTMENT

Intermediate Macroeconomics, Fall 2019 (Oct. 7)
Min Kim



- Min Kim

- 3rd year PhD student

- email: min.kim@rutgers.edu

- office hours: 13:30-14:30 on Tuesdays at 423 in NJ hall

- will do 16 lectures, while professor is on parental leave

- We will cover

- chapter 4: Savings – Investment diagram

- chapters 9-13: Aggregate Demand – Supply framework

- Let's start with warm-ups

Quick review

- In economics, we like to use a function to describe the relationships between the variables of interest

$$Y = f(X)$$

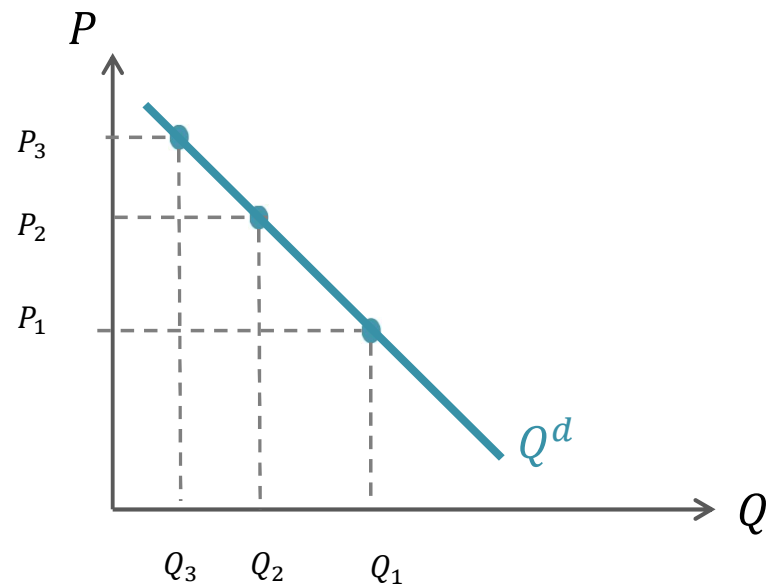
- ▣ variable Y moves with variable X through $f(\cdot)$
- For example, a demand curve Q^d :

$$Q = a - bP \text{ for some } a, b > 0$$

- ▣ b : responsiveness to the price change
- ▣ a : income, expectations, preferences, prices of other goods, etc.

Quick review

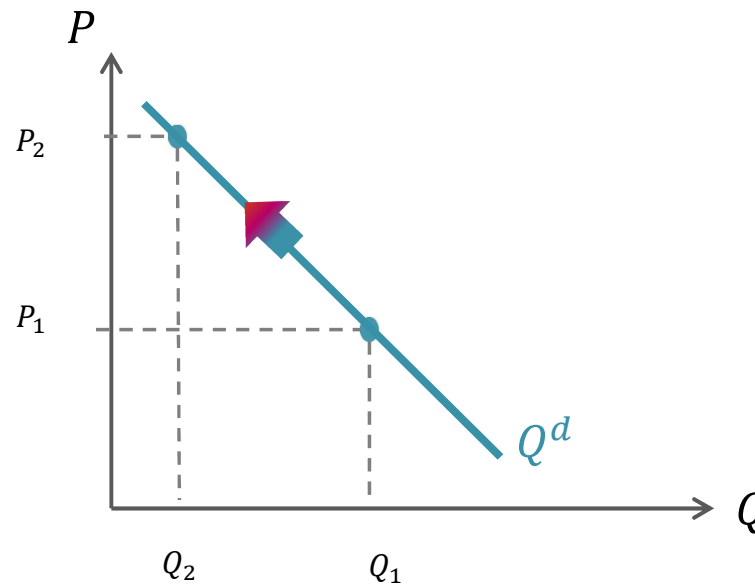
- The graph for the inverse demand curve $P = \frac{a}{b} - \frac{1}{b}Q$ is



- Two concepts:
 - ▣ movements along the curve
 - ▣ shifts of the curve

Movements along the curve

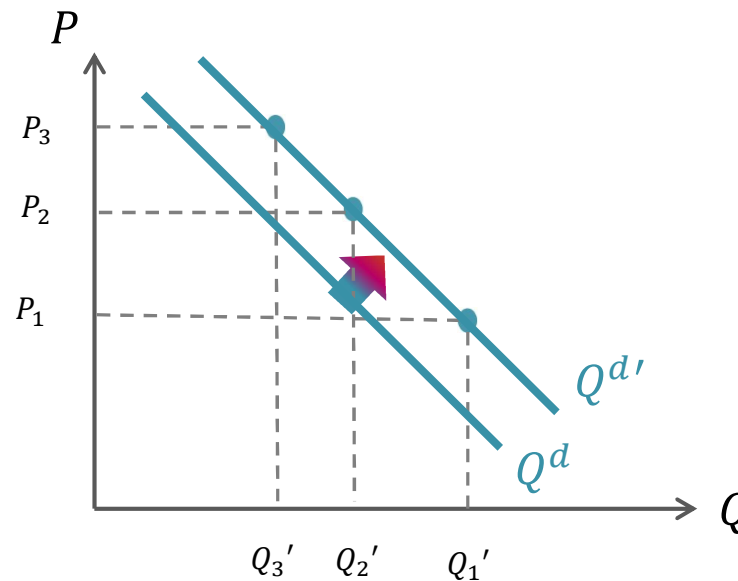
- How does Q change as P changes?



- When the price increases from P_1 to P_2 , the quantity demanded decreases, from Q_1 to Q_2

Shifts of the curve

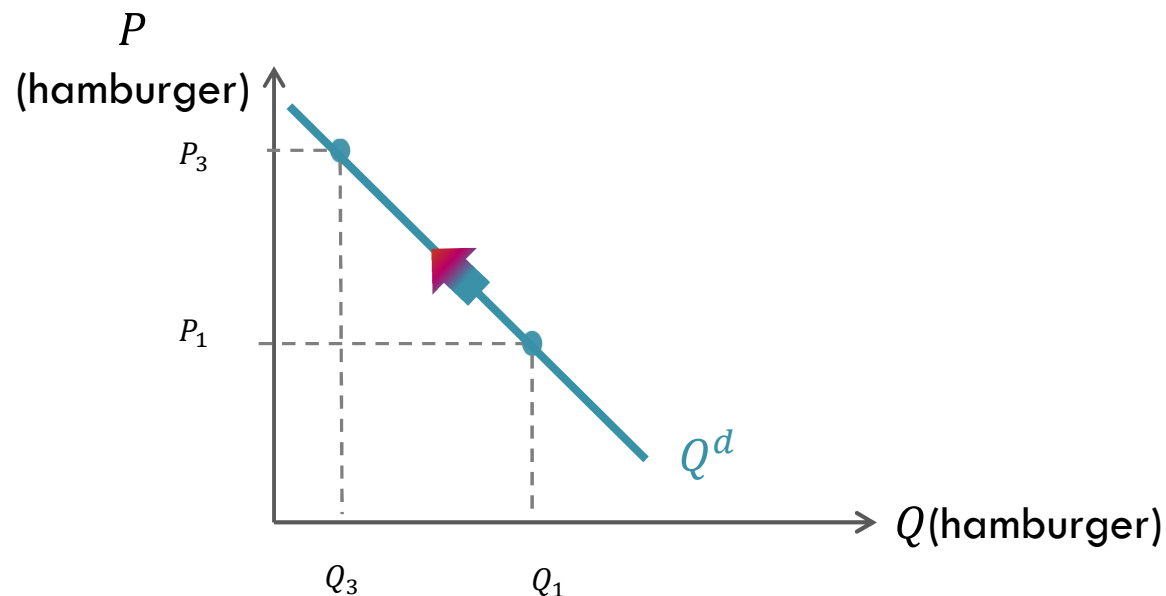
- What happens if a changes?
 - ▣ Suppose that there is an increase in income so that a increases



- ▣ the curve shifts outwards parallelly, assuming it is a normal good

Example: hamburger, ketchup, and chicken

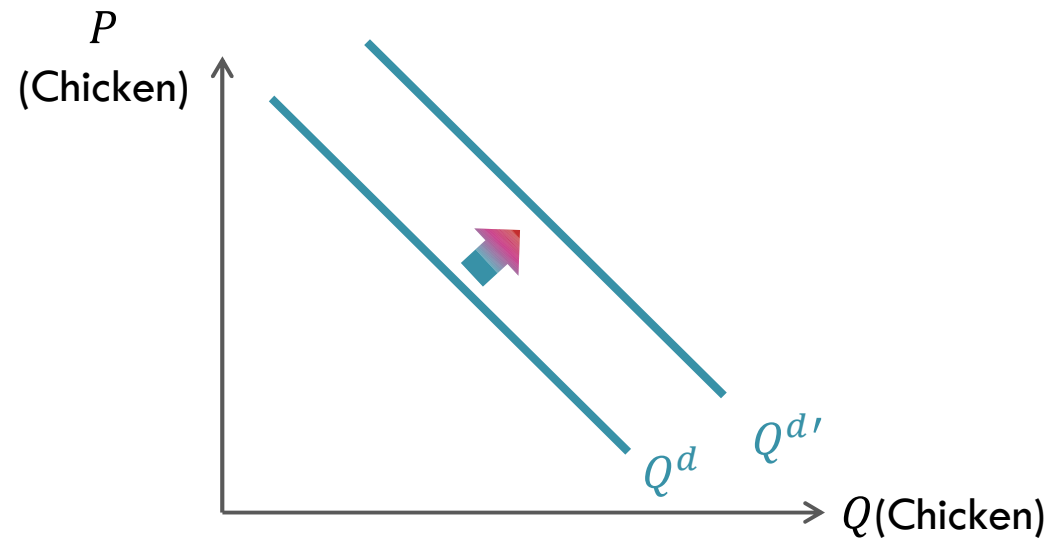
- Suppose that the price for hamburger rises
 - ▣ What happens to the demand for chicken (substitute good) and the demand for ketchup (complementary good)?



- ▣ the quantity demanded for hamburger decreases (along the curve)

Example: hamburger, ketchup, and chicken

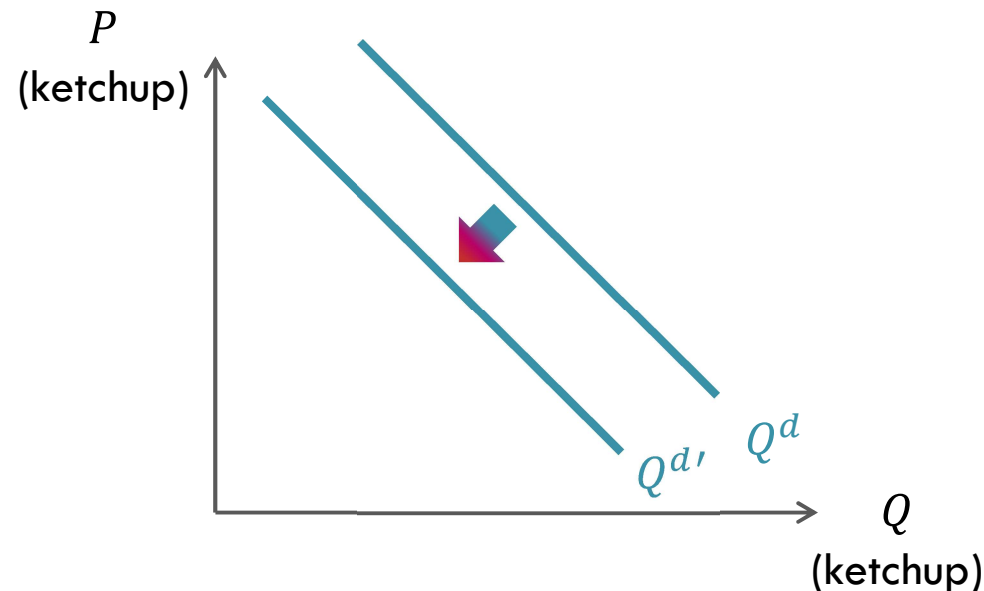
- Demand for chicken (substitute good) increases



- ▣ the demand curve shifts outwards
 - this can be interpreted as a increases

Example: hamburger, ketchup, and chicken

- Demand for ketchup (complementary good) decreases



- ▣ the demand curve shifts downwards
 - this can be interpreted as a decreases

What we have done so far

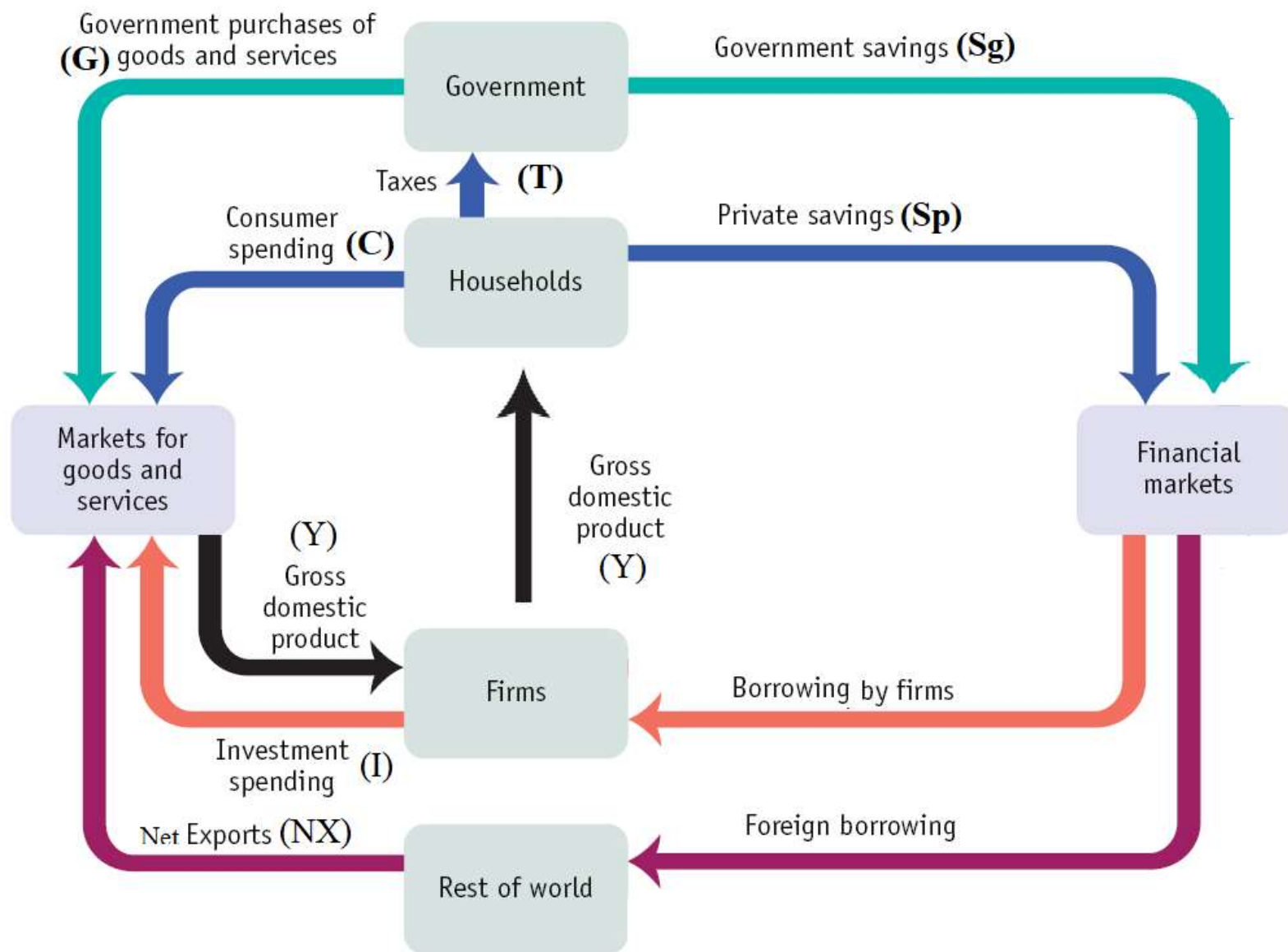
- What should we look at to know about the economy?
 - ▣ what are the important macro variables?
- Among others, main interest is real GDP, Y
 - ▣ that summarizes how well the economy is doing
- *Chapter 2*: How can we measure Y ?
 - ▣ total production = total expenditure = total income
- *Chapter 3*: What determines Y ?
 - ▣ assuming the aggregate production function: $Y = AK^bL^{1-b}$


- *Chapters 6 and 7: How does Y grow over time?*
 - ▣ in the long-run, the economy converges to the steady state k^* , which depends on A, b, n, δ and s
 - ▣ *assuming* $S = sY$ for some fixed saving rate s and $I = S$

- What is missing?
 - ▣ economy does not work mechanically
 - $S = sY$ is a strong assumption and how $I = S$?
 - ▣ agents make decisions and interact in the markets
 - households/firms/government/rest-of-world

- We assume that the output is fixed $Y = F(\bar{K}, \bar{L}) = \bar{Y}$
 - ▣ and we will focus on goods and financial markets

Flow diagram



- 
- What is the (general) equilibrium of the economy?
 - ▣ *supply=demand* in all markets (goods and financial markets)

- Walras' law says
 - ▣ *"if all other markets in an economy are in equilibrium, then that specific market must also be in equilibrium"*

- We will look for the equilibrium in goods market

$$Y = C + I + G + NX$$

- ▣ so that financial market is also in equilibrium

Outline of Chapter 4



- Consumption, saving, and investment
 - ▣ the *uses of saving identity*

- Equilibrium in three cases:
 - ▣ a closed economy
 - ▣ a small open economy
 - ▣ a large open economy

- Some exercises
 - ▣ the “global savings glut”

Consumption

- **Consumption** expenditure depends on many factors
- We separate these factors into three categories:

$$C = \bar{C} + C(Y - T, r)$$

+ -

- where:

$Y - T$ = disposable income

r = real interest rate

\bar{C} = autonomous consumption
(*i.e.*, everything else)

Recall from Chapter 2

- A **nominal interest rate** is the cost of borrowing, or the price paid for the rental of funds
 - ▣ if you borrow \$100 at 2% interest for one year
 - ▣ As a borrower, you will have to pay back \$102
- The **real interest rate** is an interest rate adjusted for changes in prices, measures purchasing power
 - ▣ suppose now that the expected inflation is 2%
 - dollars will be worth 2% less, so the *real* cost of borrowing (or the real interest rate) is 0%.
 - the amount of goods you can buy with \$100 today is the same as the amount you can buy with \$102 next year
 - no change in terms of *purchasing power*

Why does C depend negatively on r ?

- r is a relative price
 - ▣ current consumption vs. future consumption
- Example: buying a new TV today vs. in one year
 - ▣ suppose price is \$500 in both years (no inflation)
 - ▣ current cost of TV today is \$500
 - ▣ what is the *current* cost of TV in one year?
 - how much you need to save today?

- Let x be the amount you need to save

$$x(1 + r) = \$500 \quad \text{or} \quad x = \frac{\$500}{1 + r}$$

- when $r = 1\%$ $\Rightarrow x = \frac{\$500}{1.01} \approx \495

- When r increases to 10% $\Rightarrow x = \frac{\$500}{1.10} \approx \455

\Rightarrow current consumption is relatively more expensive

From consumption to saving

- Private saving is disposable income minus consumption


$$S_P = Y - T - C$$

- Govt. saving is tax revenue minus govt. expenditure

$$S_G = T - G$$

- **National saving** is S_P plus S_G

$$S = Y - C - G$$



- Output: $Y = F(\bar{K}, \bar{L}) = \bar{Y}$

- Fiscal policy is exogenous: $G = \bar{G}$ and $T = \bar{T}$
 - ▣ it does not depend on r

- Consumption: $C = \bar{C} + C(Y - T, r)$

- Then:

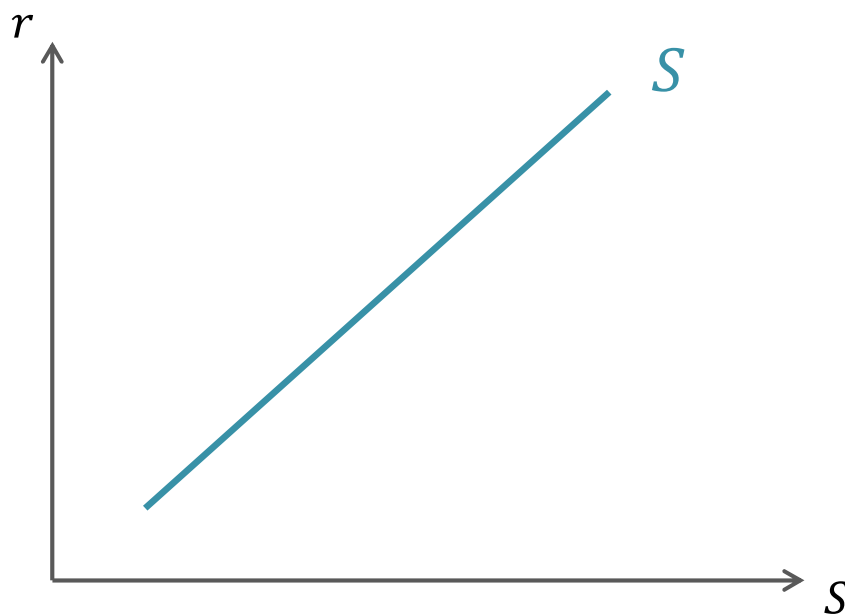
$$S = \bar{Y} - \bar{C} - C(\bar{Y} - \bar{T}, r) - \bar{G}$$

- ▣ an increasing function of the real interest rate r

Graphically,

- **National saving** is:

$$S = \bar{Y} - \bar{C} - C(\bar{Y} - \bar{T}, r) - \bar{G}$$



Investment

- Recall: **investment** is expenditure on currently produced capital goods ...
 - ▣ ... that are used to produce other goods over an extended period of time

- Assume:
$$I = \bar{I} + I(\underline{r})$$

where \bar{I} = autonomous investment

- Why is investment decreasing in r ?

- Example: firm is considering buying a new machine

- ▣ costs \$100,000

- ▣ will produce benefit of \$5,000 per year (forever)

Q: should the firm buy the machine?

- Suppose firm can borrow \$100,000 at interest rate r

- ▣ annual interest cost = $(r) \times \$100,000$

- ▣ If $r = 10\%$ \longrightarrow annual cost = \$10,000 \longrightarrow do not buy

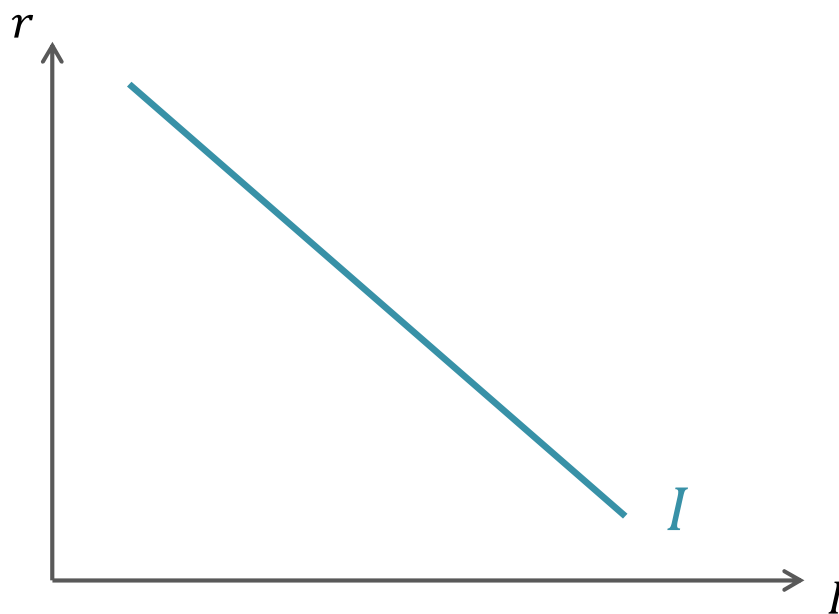
- ▣ if $r = 3\%$ \longrightarrow annual cost = \$3,000 \longrightarrow buy

- ▣ an decreasing function of the real interest rate r

Graphically,

- **Investment** is:

$$I = \bar{I} + I(r)$$



Relating saving to investment

- National saving:

$$S = Y - C - G$$

- Imposing the equilibrium condition in goods market

$$Y = C + I + G + NX$$

- Then

$$S = (C + I + G + NX) - C - G$$

or

$$S = I + NX$$

the “uses of saving” identity

Implications

- Use of national savings (S)
 - ▣ Invest in capital goods (I)
 - ▣ Sell goods to foreigners for foreign currency assets (NX)
 - $S - I$ is called *net capital outflow*
- Goods market is in **equilibrium** if $S = I + NX$
 - ▣ by Walras' law, financial market is also in equilibrium
- If $S \neq I + NX$, there will be some "adjustments"
 - ▣ so that the economy is in equilibrium

Adding up

- Rewrite our identity as

$$S = I + NX \quad \Rightarrow \quad S - I = \text{Export} - \text{Import}$$

- This identity holds for every country in equilibrium:

$$S_{US} - I_{US} = \text{Export}_{US} - \text{Import}_{US}$$

$$S_{Canada} - I_{Canada} = \text{Export}_{Canada} - \text{Import}_{Canada}$$

$$S_{Mexico} - I_{Mexico} = \text{Export}_{Mexico} - \text{Import}_{Mexico}$$

...

- Adding across all countries in the world:

$$\sum_i S_i - \sum_i I_i = \sum_i \text{Export}_i - \sum_i \text{Import}_i$$

□ Repeating:

$$\sum_i S_i - \sum_i I_i = \sum_i Export_i - \sum_i Import_i$$

total saving in the world

total investment in the world

total exports

total imports

Q: How are these related?

A: total exports = total imports

(every good exported from one country is imported to another)

□ Result:

$$\sum_i S_i - \sum_i I_i = 0 \quad \text{or} \quad \begin{array}{c} \text{total} \\ \text{saving} \\ \text{in the} \\ \text{world} \end{array} = \begin{array}{c} \text{total} \\ \text{investment} \\ \text{in the} \\ \text{world} \end{array}$$

Outline of Chapter 4



- Consumption, saving, and investment
 - ▣ the *uses of saving identity*
- **Equilibrium in three cases:**
 - ▣ a closed economy
 - ▣ a small open economy
 - ▣ a large open economy
- Some exercises
 - ▣ the “global savings glut”

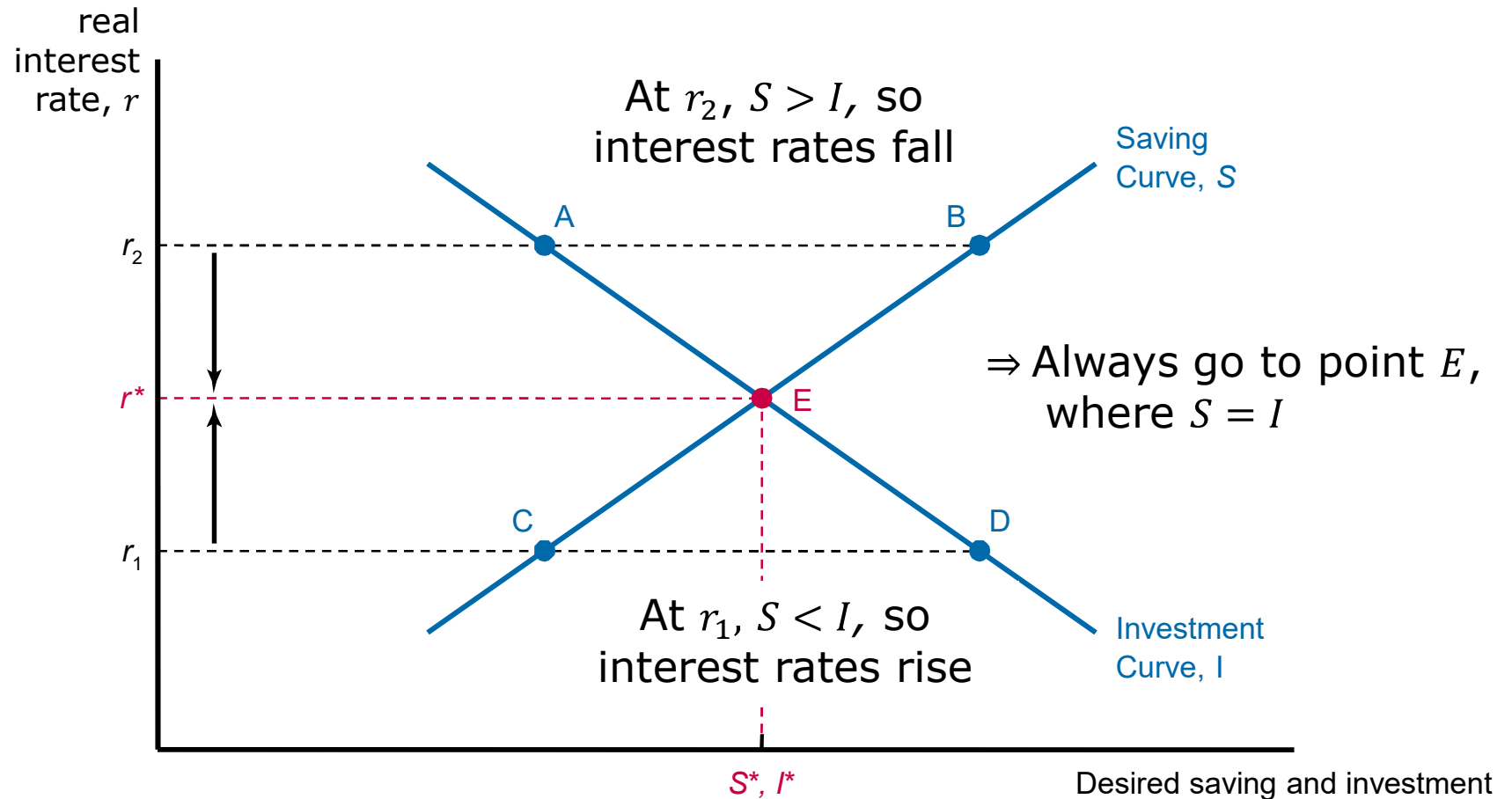
1) A closed economy

- Suppose there is *no* international trade
 - ▣ then NX must equal zero
 - ▣ and $S = I$ must hold in equilibrium

- Two interpretations:
 - ▣ we are looking at an economically closed country
 - ▣ we are looking at the world as a whole

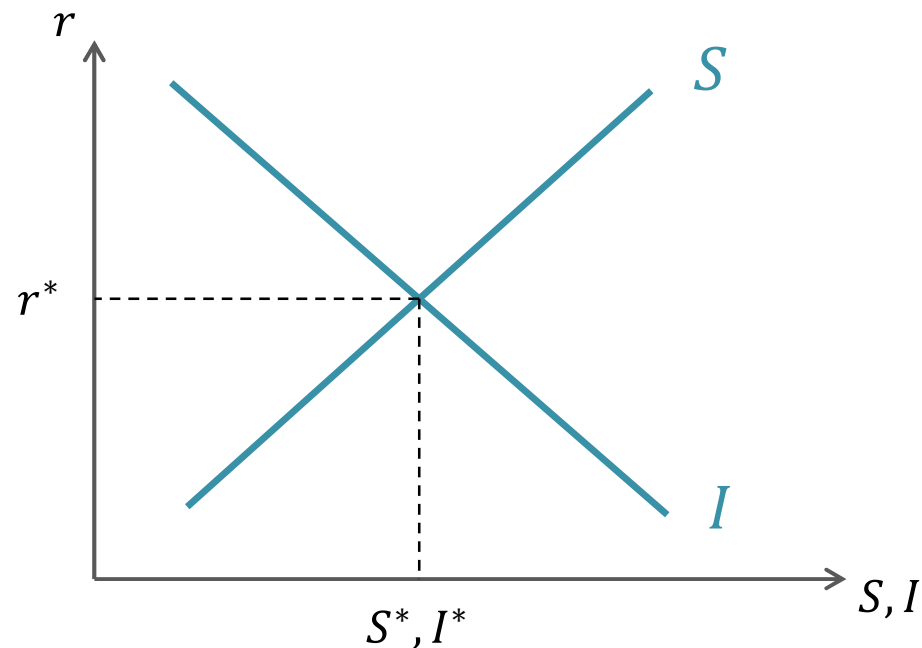
- Real interest rate r is determined by local forces
 - ▣ supply (of saving) and demand (for investment)

Equilibrium in a closed economy



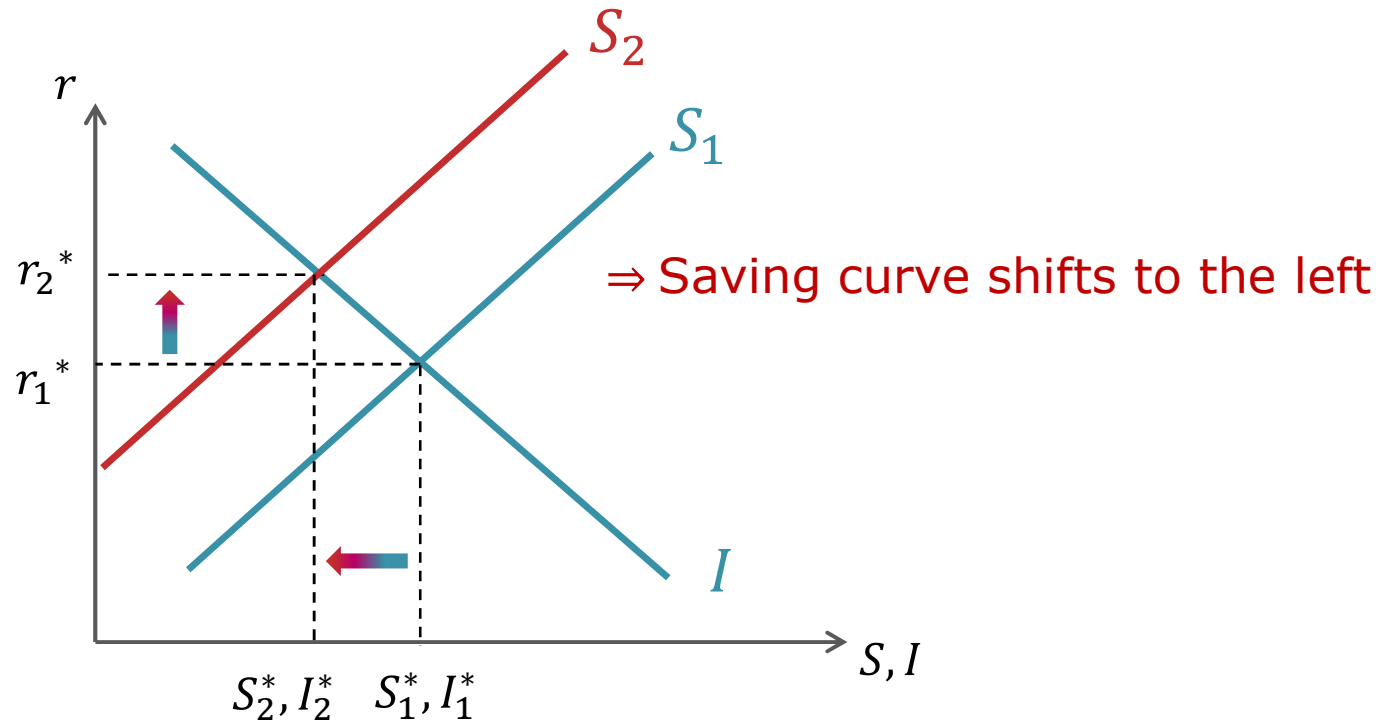
Increase in government spending ($\bar{G} \uparrow$)

- will decrease national saving $S = \bar{Y} - \bar{C} - c(\bar{Y} - \bar{T}, r) - \bar{G}$



Increase in government spending ($\bar{G} \uparrow$)

- will decrease national saving $s = \bar{Y} - \bar{C} - c(\bar{Y} - \bar{T}, r) - \bar{G}$



- Equilibrium level of saving and investment fall
 - this is called **crowding out effect**
 - criticism to fiscal stimulus package by the government